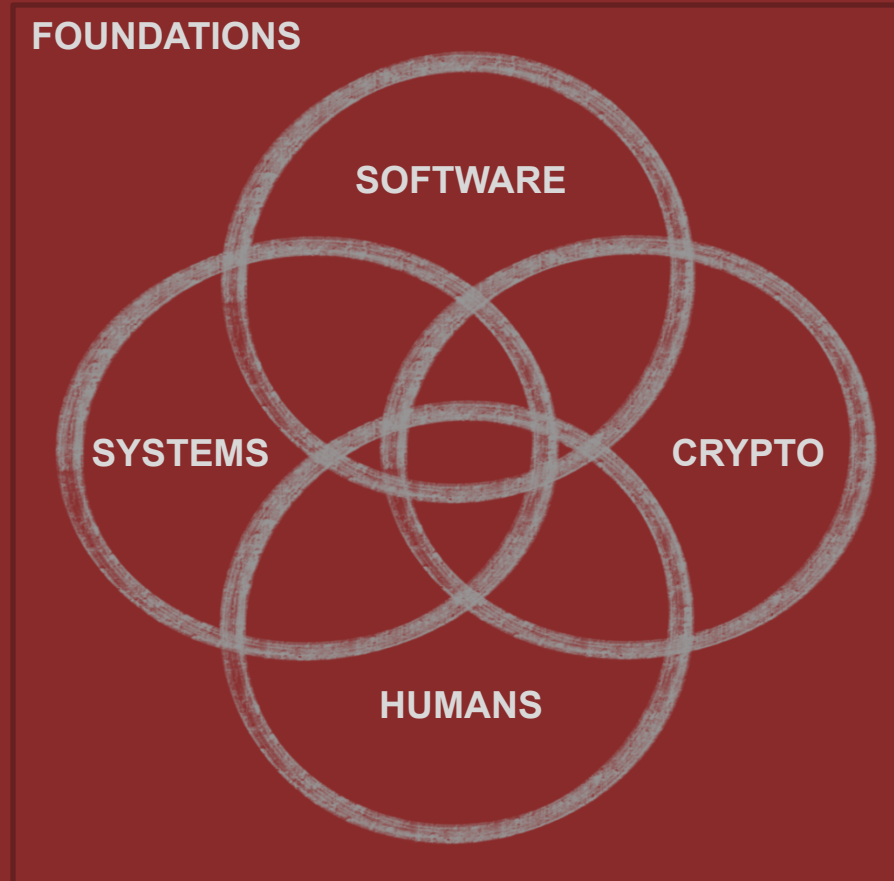


Διάλεξη #17 - Authenticated Encryption and Asymmetric Crypto

Εθνικό και Καποδιστριακό Πανεπιστήμιο Αθηνών

Εισαγωγή στην Ασφάλεια

Θανάσης Αυγερινός



Huge thank you to [David Brumley](#) from Carnegie Mellon University for the guidance and content input while developing this class (lots of slides from Dan Boneh @ Stanford!)

Την προηγούμενη φορά

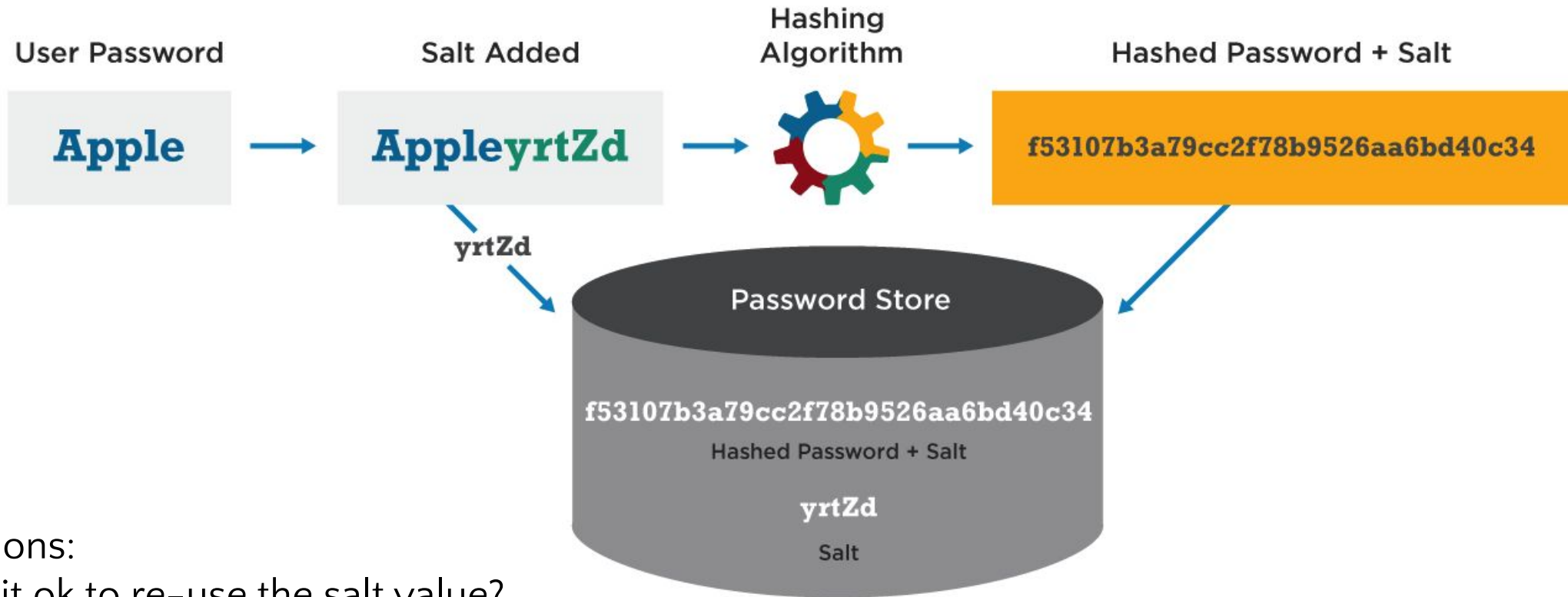
- Hashes Intro
- Hash Constructions
- HMAC
- Hash Tricks/Datastructures

Ανακοινώσεις / Διευκρινίσεις

- Πως λειτουργεί το password salt;

Password Salt

Password Hash Salting



Questions:

1. Is it ok to re-use the salt value?
2. Is it ok to use a 3-bit salt value?

No!

Σήμερα

- Authenticated Encryption (AuthEnc)
- Asymmetric/Public Key Cryptography
 - Merkle's Puzzles
 - Diffie-Hellman
 - RSA



Hopefully!



Authenticated Encryption

Recap: the story so far

Confidentiality: semantic security against a CPA attack

- Encryption secure against **eavesdropping only**

Integrity:

- Existential unforgeability under a chosen message attack
- CBC-MAC, HMAC, *MAC

Can we combine them: encryption secure against **tampering**

- Ensuring both confidentiality and integrity

... but first, some history

Authenticated Encryption (AE): introduced in 2000 [KY'00, BN'00]

Crypto APIs before then: (e.g. MS-CAPI)

- Provide API for CPA-secure encryption (e.g. CBC with rand. IV)
- Provide API for MAC (e.g. HMAC)

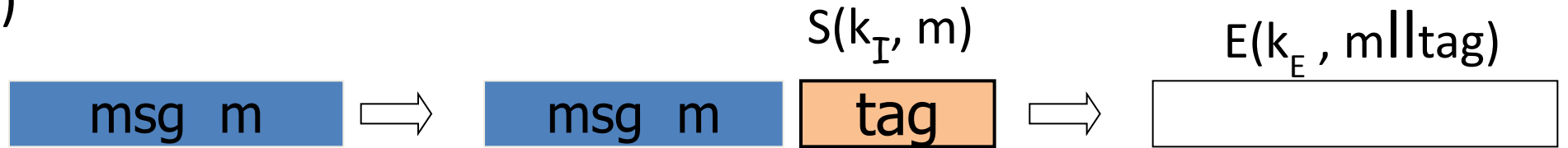
Every project had to combine the two itself without a well defined goal

- Not all combinations provide AE ...

Combining MAC and ENC (CCA)

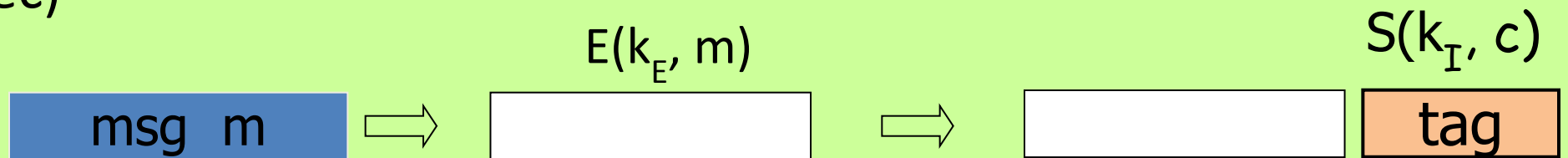
Encryption key k_E . MAC key = k_I

Option 1: (SSL)

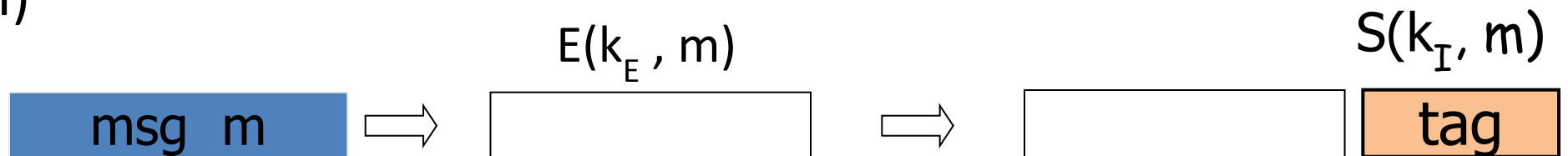


Option 2: (IPsec)

**always
correct**



Option 3: (SSH)



A.E. Theorems

Let (E,D) be CPA secure cipher and (S,V) secure MAC. Then:

1. Encrypt-then-MAC: always provides A.E.

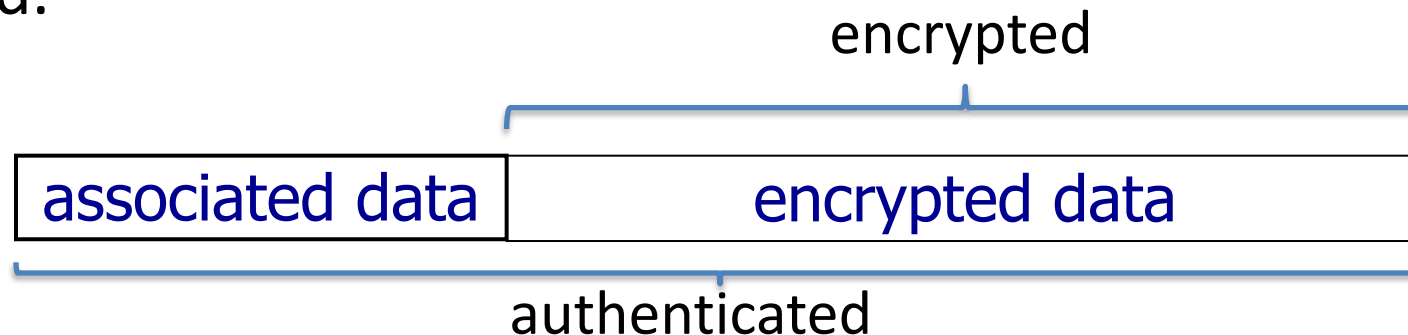
1. MAC-then-encrypt: may be insecure against CCA attacks

however: when (E,D) is rand-CTR mode or rand-CBC
M-then-E provides A.E.

Standards (at a high level)

- **GCM:** CTR mode encryption then CW-MAC
(accelerated via Intel's PCLMULQDQ instruction)
- **CCM:** CBC-MAC then CTR mode encryption (802.11i)
- **EAX:** CTR mode encryption then CMAC

All support AEAD: (auth. enc. with associated data). All are nonce-based.

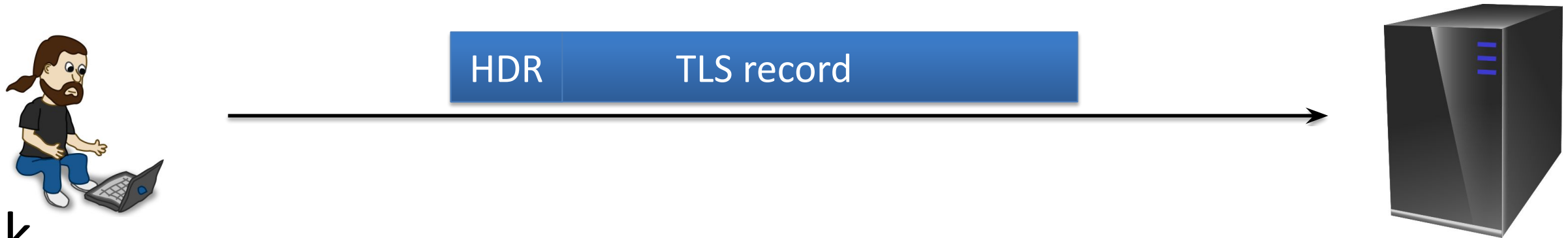


An example API (OpenSSL)

```
int AES_GCM_Init(AES_GCM_CTX *ain,  
    unsigned char *nonce, unsigned long noncelen,  
    unsigned char *key, unsigned int klen )
```

```
int AES_GCM_EncryptUpdate(AES_GCM_CTX *a,  
    unsigned char *aad, unsigned long aadlen,  
    unsigned char *data, unsigned long datalen,  
    unsigned char *out, unsigned long *outlen)
```

The TLS Record Protocol (TLS 1.2)



$k_{b \rightarrow s'}$

$k_{s \rightarrow b}$

Unidirectional keys:

$k_{b \rightarrow s}$ and $k_{s \rightarrow b}$

$k_{b \rightarrow s'}$

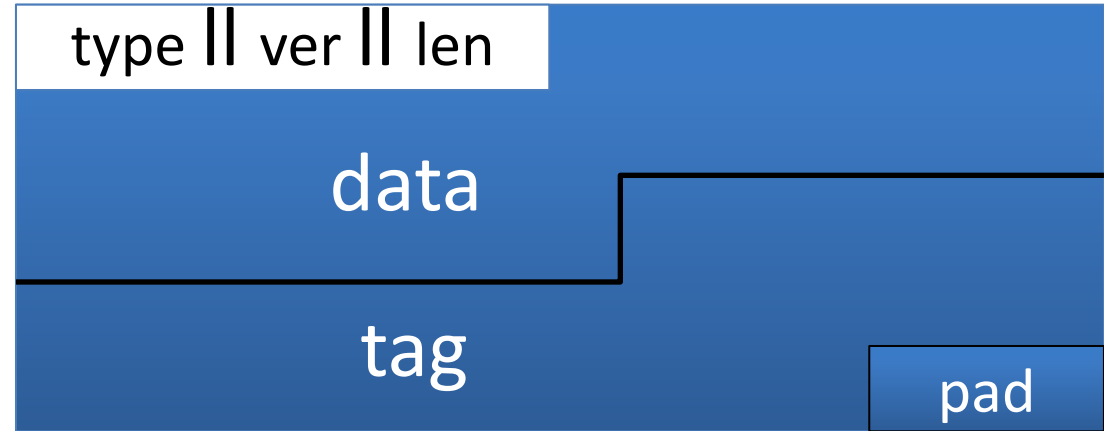
$k_{s \rightarrow b}$

Stateful encryption:

- Each side maintains two 64-bit counters: $ctr_{b \rightarrow s}$, $ctr_{s \rightarrow b}$
- Init. to 0 when session started. $ctr++$ for every record.
- Purpose: replay defense

TLS record: encryption (CBC AES-128, HMAC-SHA1)

$$k_{b \rightarrow s} = (k_{\text{mac}}, k_{\text{enc}})$$



Browser side $\text{enc}(k_{b \rightarrow s}, \text{data}, \text{ctr}_{b \rightarrow s})$:

step 1: $\text{tag} \leftarrow S(k_{\text{mac}}, [++\text{ctr}_{b \rightarrow s} \parallel \text{header} \parallel \text{data}])$

step 2: pad $[\text{header} \parallel \text{data} \parallel \text{tag}]$ to AES block size

step 3: CBC encrypt with k_{enc} and new random IV

step 4: prepend header

TLS record: decryption (CBC AES-128, HMAC-SHA1)

Server side $\text{dec}(k_{b \rightarrow s}, \text{record}, \text{ctr}_{b \rightarrow s})$:

step 1: CBC decrypt record using k_{enc}

step 2: check pad format: send **bad_record_mac** if invalid

step 3: check tag on $[++\text{ctr}_{b \rightarrow s} \parallel \text{header} \parallel \text{data}]$

send **bad_record_mac** if invalid

Provides authenticated encryption

(provided no other info. is leaked during decryption)

Bugs in older versions (prior to TLS 1.1)

IV for CBC is predictable: (chained IV)

IV for next record is last ciphertext block of current record.

Not CPA secure. (a practical exploit: BEAST attack)

Padding oracle: during decryption

if pad is invalid send **decryption failed** alert

if mac is invalid send **bad_record_mac** alert

⇒ attacker learns info. about plaintext (various attacks possible)

Lesson: when decryption fails, do not explain why

Leaking the length

The TLS header leaks the length of TLS records

- Lengths can also be inferred by observing network traffic

For many web applications, leaking lengths reveals sensitive info:

- In tax preparation sites, lengths indicate the type of return being filed which leaks information about the user's income
- In healthcare sites, lengths leaks what page the user is viewing
- In Google maps, lengths leaks the location being requested

No easy solution



**Asymmetric / Public
Key Cryptography**

Key management

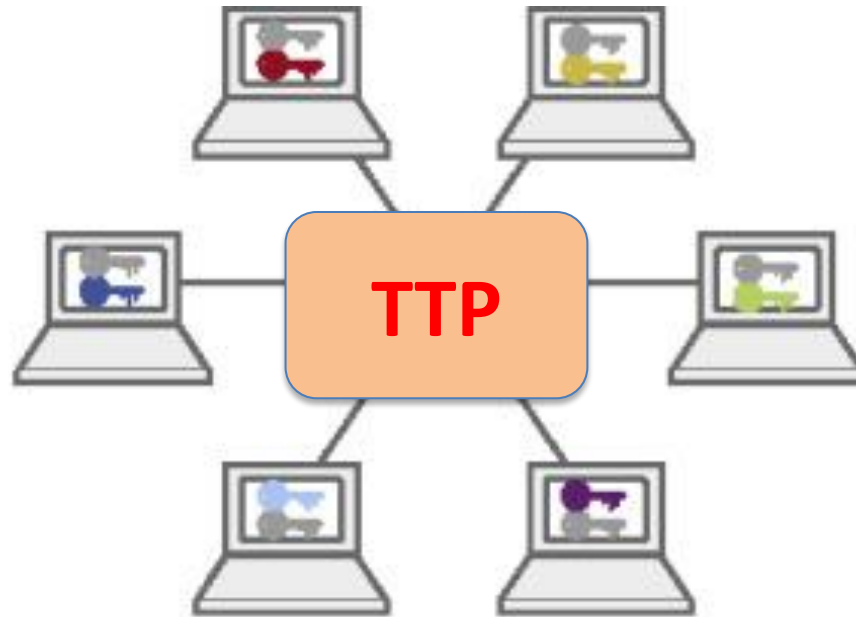
Problem: n users. Storing mutual secret keys is difficult



Total: $O(n)$ keys per user

A better solution

Online Trusted 3rd Party (TTP)

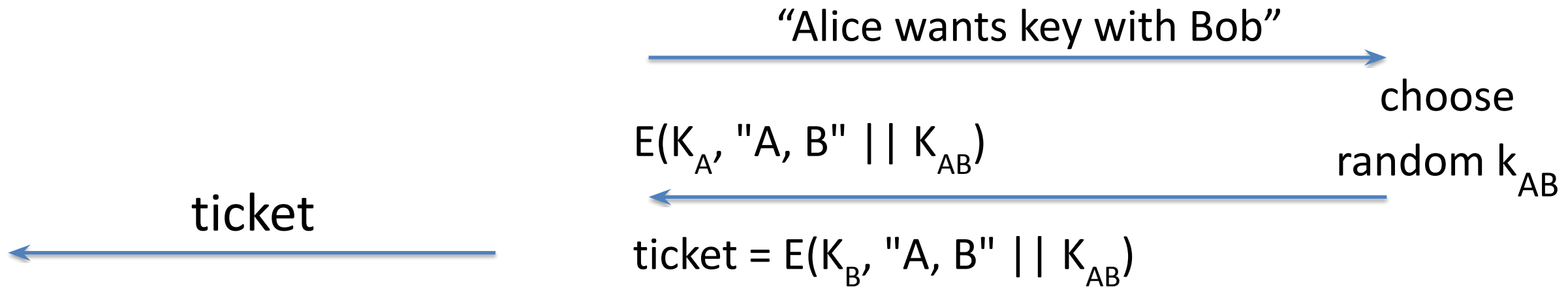


Generating keys: a toy protocol

Alice wants a shared key with Bob. Eavesdropping security only.

Bob (k_B) Alice (k_A)

TTP



k_{AB}

k_{AB}

(E,D) a CPA-secure cipher

Generating keys: a toy protocol

Alice wants a shared key with Bob. Eavesdropping security only.

Eavesdropper sees: $E(k_A, \text{"A, B"} \parallel k_{AB})$; $E(k_B, \text{"A, B"} \parallel k_{AB})$

(E,D) is CPA-secure \Rightarrow
eavesdropper learns nothing about k_{AB}

Note: TTP needed for every key exchange, knows all session keys.

(basis of Kerberos system)

Toy protocol: insecure against active attacks

Example: insecure against replay attacks

Attacker records session between Alice and merchant Bob

- For example a book order

Attacker replays session to Bob

- Bob thinks Alice is ordering another copy of book

Key question

Can we generate shared keys without an **online** trusted 3rd party?

Answer: yes!

Starting point of public-key cryptography:

- Merkle (1974), Diffie-Hellman (1976), RSA (1977)
- More recently: ID-based enc. (BF 2001), Functional enc. (BSW 2011)

Merkle Puzzles

Key exchange without an online TTP?

Goal: Alice and Bob want shared key, unknown to eavesdropper

- For now: security against eavesdropping only (no tampering)



Can this be done using generic symmetric crypto?

Merkle Puzzles (1974)

Answer: yes, but very inefficient

Main tool: puzzles

- Problems that can be solved with some effort
- Example: $E(k,m)$ a symmetric cipher with $k \in \{0,1\}^{128}$
 - **puzzle(P) = E(P, “message”)** where $P = 0^{96} \parallel b_1 \dots b_{32}$
 - Goal: find P by trying all 2^{32} possibilities

Merkle puzzles

Alice: prepare 2^{32} puzzles

- For $i=1, \dots, 2^{32}$ choose random $P_i \in \{0,1\}^{32}$ and $x_i, k_i \in \{0,1\}^{128}$

set $\text{puzzle}_i \leftarrow E(0^{96} \parallel P_i, \text{"Puzzle \# } x_i \text{"} \parallel k_i)$

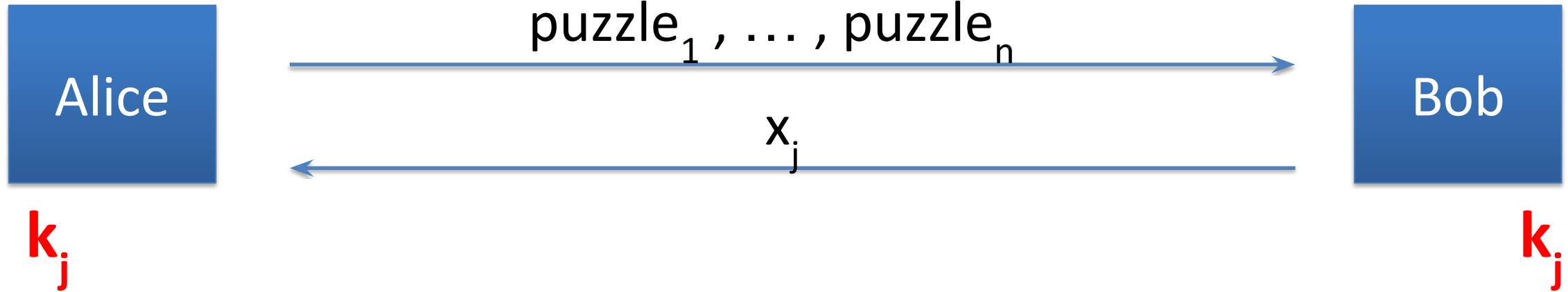
- Send $\text{puzzle}_1, \dots, \text{puzzle}_{2^{32}}$ to Bob

Bob: choose a random puzzle_j and solve it. Obtain (x_j, k_j) .

- Send x_j to Alice

Alice: lookup puzzle with number x_j . Use k_j as shared secret

In a figure



Alice's work: $O(n)$ (prepare n puzzles)

Bob's work: $O(n)$ (solve one puzzle)

Eavesdropper's work:  (e.g. 2^{64} time)

Impossibility Result

Can we achieve a better gap using a general symmetric cipher?

Answer: unknown

But: roughly speaking,

quadratic gap is best possible if we treat cipher as
a black box oracle [IR'89, BM'09]



The Diffie-Hellman (DH) Protocol

Key exchange without an online TTP?

Goal: Alice and Bob want shared secret, unknown to eavesdropper

- For now: security against eavesdropping only (no tampering)



Can this be done with an exponential gap?

The Diffie-Hellman protocol (informally)

Fix a large prime p (e.g. 600 digits)

Fix an integer g in $\{1, \dots, p\}$

Alice

choose random \mathbf{a} in $\{1, \dots, p-1\}$

$$A = g^a \pmod{p}$$

Bob

choose random \mathbf{b} in $\{1, \dots, p-1\}$

$$B = g^b \pmod{p}$$

$$\mathbf{B}^a \pmod{p} = (g^b)^a = \mathbf{k}_{AB} = g^{ab} \pmod{p}$$

Security (much more on this later)

Eavesdropper sees: $p, g, A=g^a \pmod{p}$, and $B=g^b \pmod{p}$

Can she compute $g^{ab} \pmod{p}$??

More generally: define $DH_g(g^a, g^b) = g^{ab} \pmod{p}$

How hard is the DH function mod p ?

How hard is the DH function mod p ?

Suppose prime p is n bits long.

Best known algorithm (GNFS): run time $\exp(\tilde{O}(\sqrt[3]{n}))$

<u>cipher key size</u>	<u>modulus size</u>	<u>Elliptic Curve size</u>
80 bits	1024 bits	160 bits
128 bits	3072 bits	256 bits
256 bits (AES)	<u>15360</u> bits	512 bits

As a result: slow transition away from (mod p) to elliptic curves



www.google.com

The identity of this website has been verified by Thawte SGC CA.

[Certificate Information](#)



Your connection to www.google.com is encrypted with 128-bit encryption.

The connection uses TLS 1.0.

The connection is encrypted using RC4_128, with SHA1 for message authentication and ECDHE_RSA as the key exchange mechanism.

Elliptic curve
Diffie-Hellman

Insecure against man-in-the-middle

As described, the protocol is insecure against **active** attacks

Alice

MiTM

Bob

$$A = g^a \pmod{p}$$


$$A' = g^{a'} \pmod{p}$$


$$B = g^b \pmod{p}$$


$$B' = g^{b'} \pmod{p}$$


$$\text{Key} = g^{ab'} \pmod{p}$$

$$\text{Key} = g^{a'b} \pmod{p}$$



Public Key Cryptography

Establishing a shared secret

Goal: Alice and Bob want shared secret, unknown to eavesdropper

- For now: security against eavesdropping only (no tampering)



This segment: a different approach

Public key encryption

Def: a public-key encryption system is a triple of algs. (G, E, D)

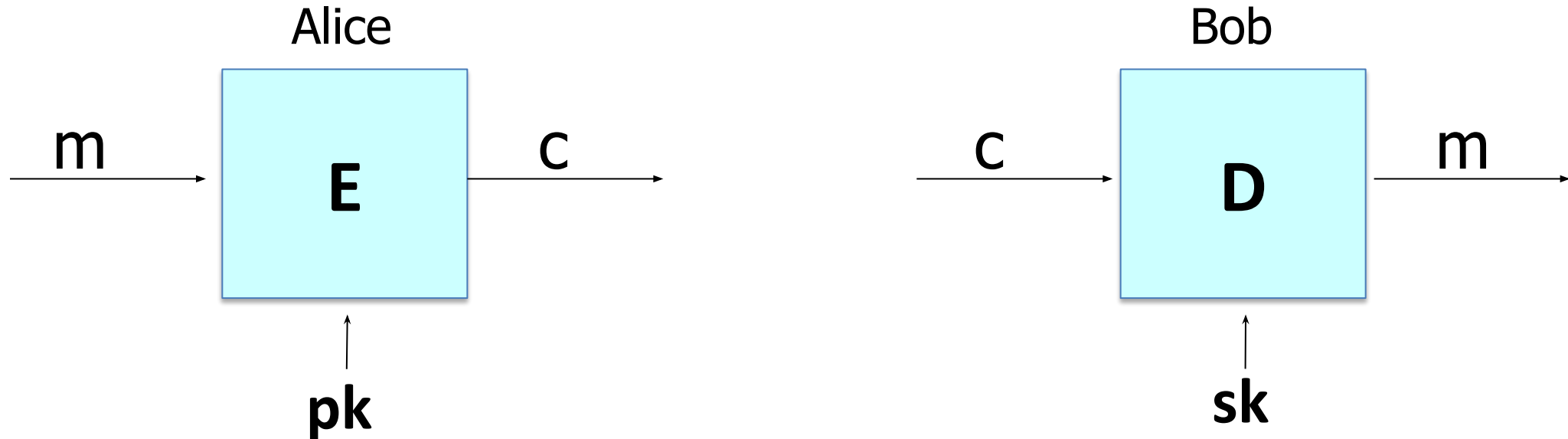
- $G()$: randomized alg. outputs a key pair (pk, sk)
- $E(pk, m)$: randomized alg. that takes $m \in M$ and outputs $c \in C$
- $D(sk, c)$: det. alg. that takes $c \in C$ and outputs $m \in M$ or \perp

Consistency: $\forall (pk, sk)$ output by G :

$$\forall m \in M: D(sk, E(pk, m)) = m$$

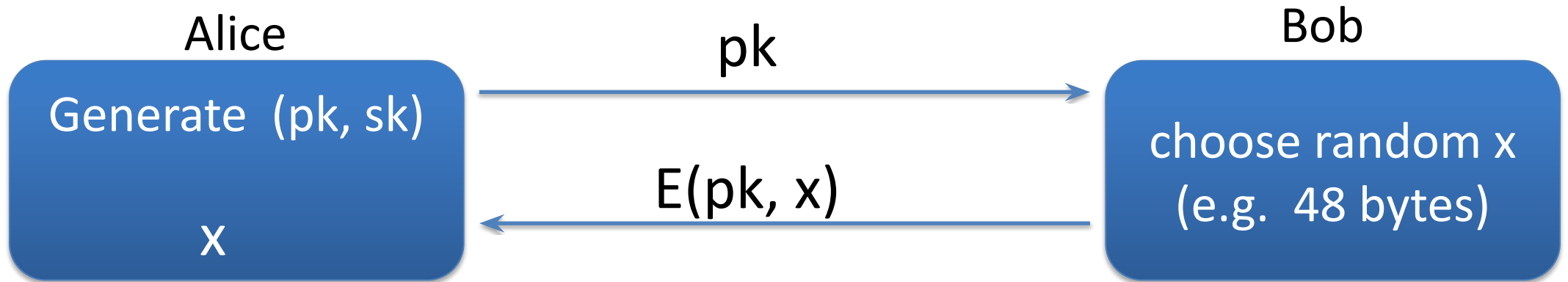
Public key encryption

Bob: generates (PK, SK) and gives PK to Alice



Applications

Session setup (for now, only eavesdropping security)



Non-interactive applications: (e.g. Email)

- Bob sends email to Alice encrypted using pk_{alice}
- Note: Bob needs pk_{alice} (public key management)

Trapdoor functions (TDF)

Def: a trapdoor func. $X \rightarrow Y$ is a triple of efficient algs. (G, F, F^{-1})

- $G()$: randomized alg. outputs a key pair (pk, sk)
- $F(pk, \cdot)$: det. alg. that defines a function $X \rightarrow Y$
- $F^{-1}(sk, \cdot)$: defines a function $Y \rightarrow X$ that inverts $F(pk, \cdot)$

More precisely: $\forall (pk, sk)$ output by G

$$\forall x \in X: F^{-1}(sk, F(pk, x)) = x$$

The RSA trapdoor permutation

First published: Scientific American, Aug. 1977.

Very widely used:

- SSL/TLS: certificates and key-exchange
- Secure e-mail and file systems
- ... many others

The RSA trapdoor permutation

G(): choose random primes $p, q \approx 1024$ bits. Set $N=pq$.

choose integers e, d s.t. $e \cdot d = 1 \pmod{\phi(N)}$ where $\phi(N) = (p - 1)(q - 1)$

output $pk = (N, e)$, $sk = (N, d)$

$$\mathbf{F}(pk, x) : \mathbb{Z}_N^* \rightarrow \mathbb{Z}_N^* ; \quad \mathbf{RSA}(x) = x^e \quad (\text{in } \mathbb{Z}_N)$$

$$\mathbf{F}^{-1}(sk, y) = y^d ; \quad y^d = \mathbf{RSA}(x)^d = x^{ed} = x^{k\phi(N)+1} = (x^{\phi(N)})^k \cdot x = x$$

The RSA Assumption

RSA assumption: RSA is one-way permutation

For all efficient algs. A :

$$\Pr \left[A(N, e, y) = y^{1/e} \right] < \text{negligible}$$

where $p, q \xleftarrow{R} n\text{-bit primes}$, $N \leftarrow pq$, $y \xleftarrow{R} \mathbb{Z}_N^*$

Review: RSA pub-key encryption (ISO std)

(E_s, D_s) : symmetric enc. scheme providing auth. encryption.

$H: Z_N \rightarrow K$ where K is key space of (E_s, D_s)

- **G()**: generate RSA params: $pk = (N, e)$, $sk = (N, d)$
- **E(pk, m)**:
 - (1) choose random x in Z_N
 - (2) $y \leftarrow \text{RSA}(x) = x^e$, $k \leftarrow H(x)$
 - (3) output $(y, E_s(k, m))$
- **D(sk, (y, c))**: output $D_s(H(\text{RSA}^{-1}(y)), c)$

Textbook RSA is insecure

Textbook RSA encryption:

- public key: (N, e) Encrypt: $c \leftarrow m^e$ (in Z_N)
- secret key: (N, d) Decrypt: $c^d \rightarrow m$

Insecure cryptosystem !!

- Is not semantically secure and many attacks exist

⇒ The RSA trapdoor permutation is not an encryption scheme !

Ευχαριστώ και καλή μέρα εύχομαι!

Keep hacking!